

# Volatility prediction on SPY product

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# PLAN

- **Part I:** Volatility estimation\*
- **Part II:** Rough volatility models
- **Part III:** Trading Strategy (risk management)

# Part I : Volatility estimation

## SPY: SPDR S&P 500 ETF Trust

- **Overview:** SPY is an exchange-traded fund (ETF) that tracks the performance of the S&P 500 Index.
- **Composition:** It holds stocks from 500 leading companies across various sectors in the U.S. economy.
- **Purpose:** Provides investors with a cost-effective and convenient way to gain broad market exposure.
- **Benefits:**
  - Diversification: Reduces risk by spreading investments across multiple companies.
  - Liquidity: Highly traded, making it easy to buy and sell.
  - Dividends: Pays dividends based on the underlying stocks.
- **Use Cases:** Suitable for both individual and institutional investors seeking to match the performance of the S&P 500.

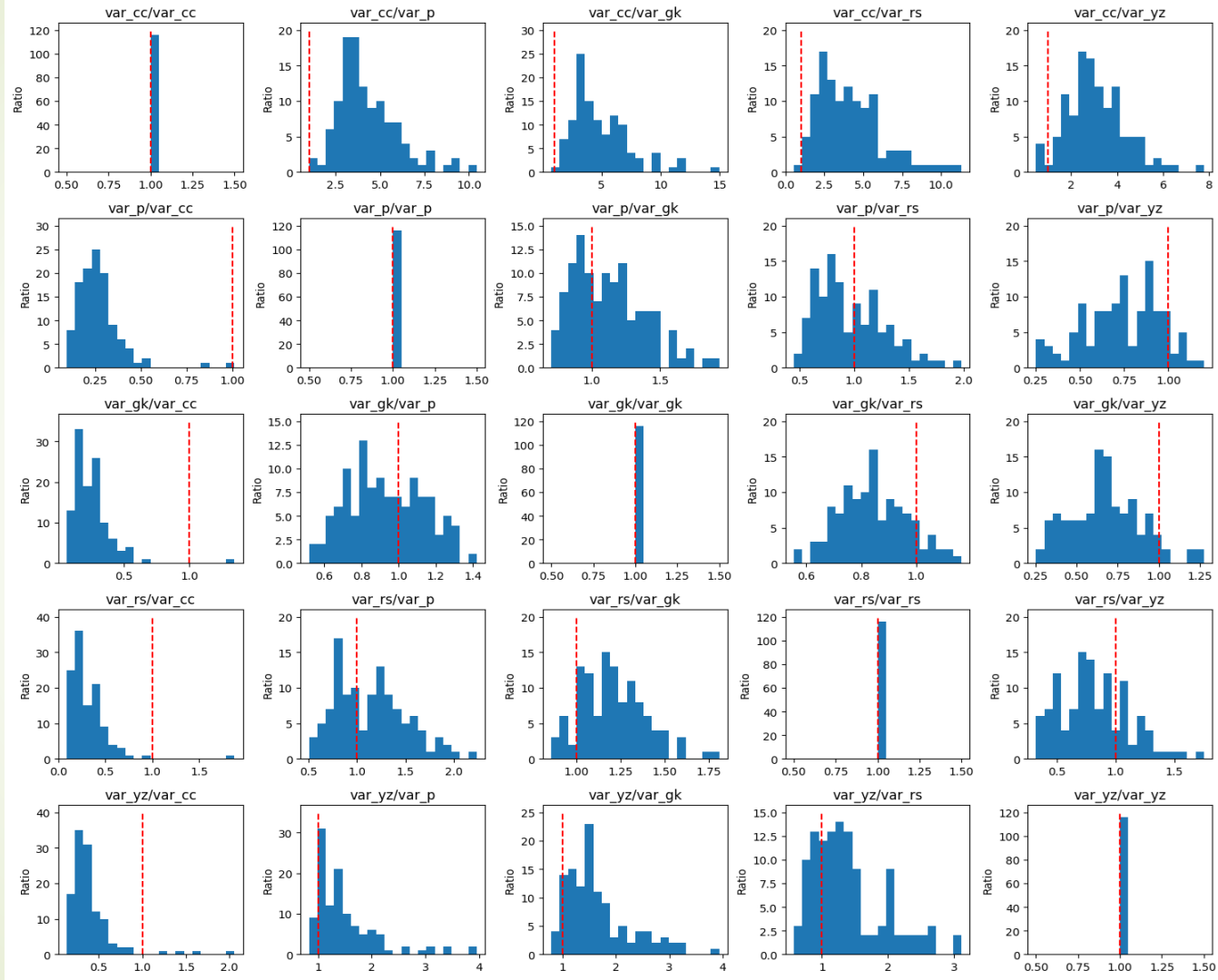
# Price development of SPY



# Efficiency Comparison Between Estimators

Best: Garman-Klass

Worst: Close-to-Close



# Volatility estimators

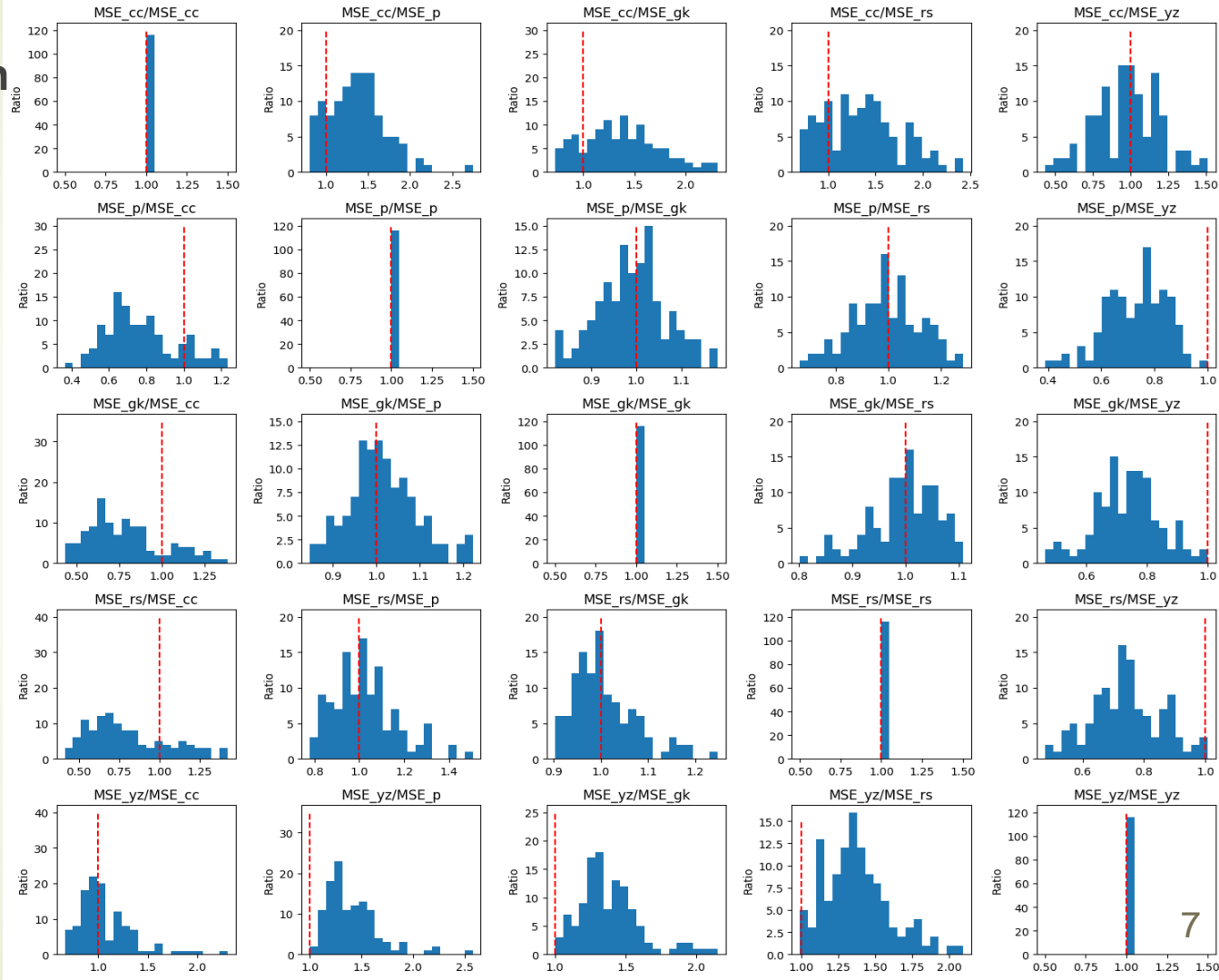
We will be compare the following estimators :

- Close-to-close volatility
- Parkinson volatility
- Garman-Klass volatility
- Rogers-Satchell volatility
- Yang-Zhang volatility

# Efficiency Comparison Between Estimators

**Best:** GK, P and RS

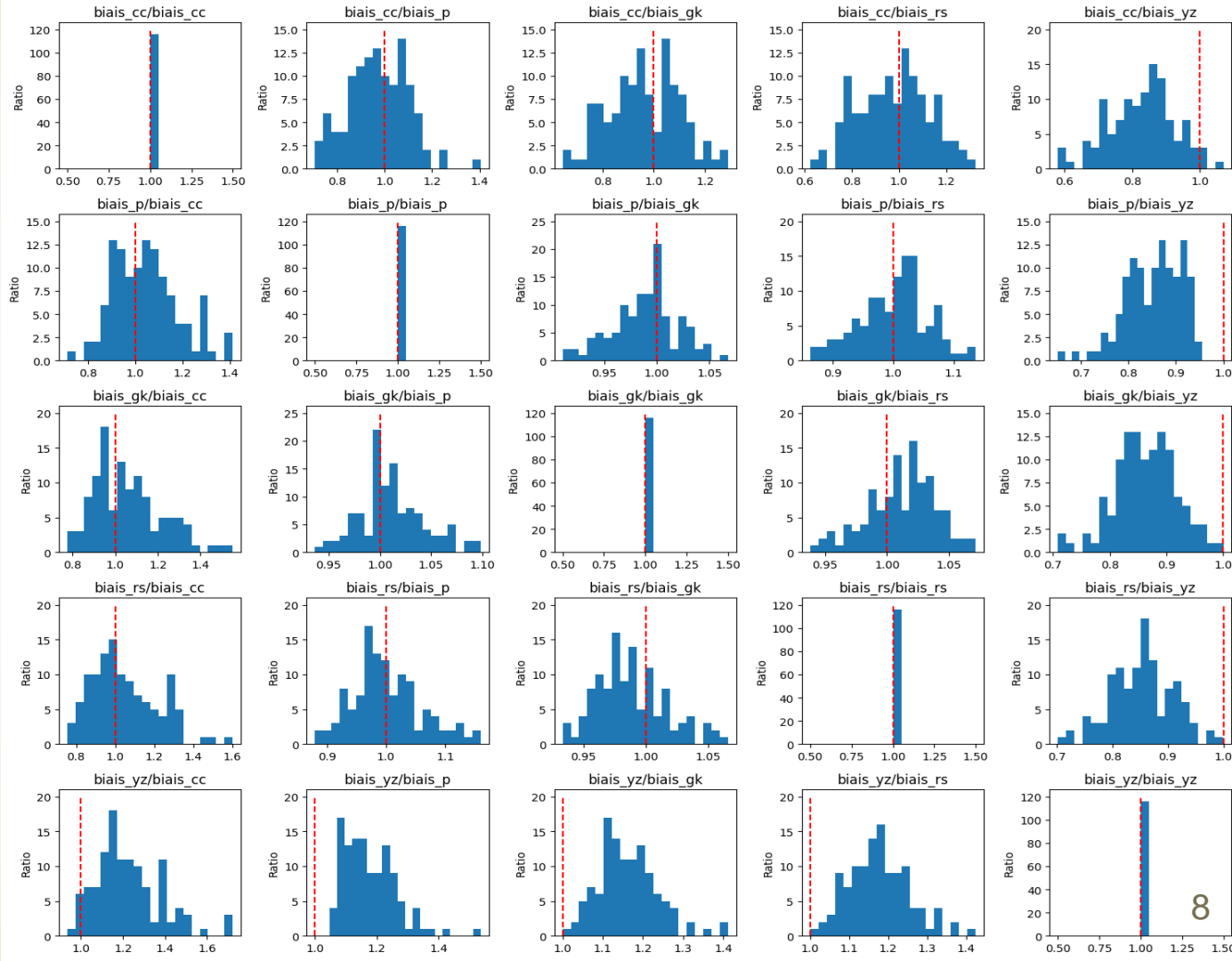
**Worst:** YZ and CC



# Stability Comparison Between Estimators

Best: P, CC and RS

Worst: Yang-Zang

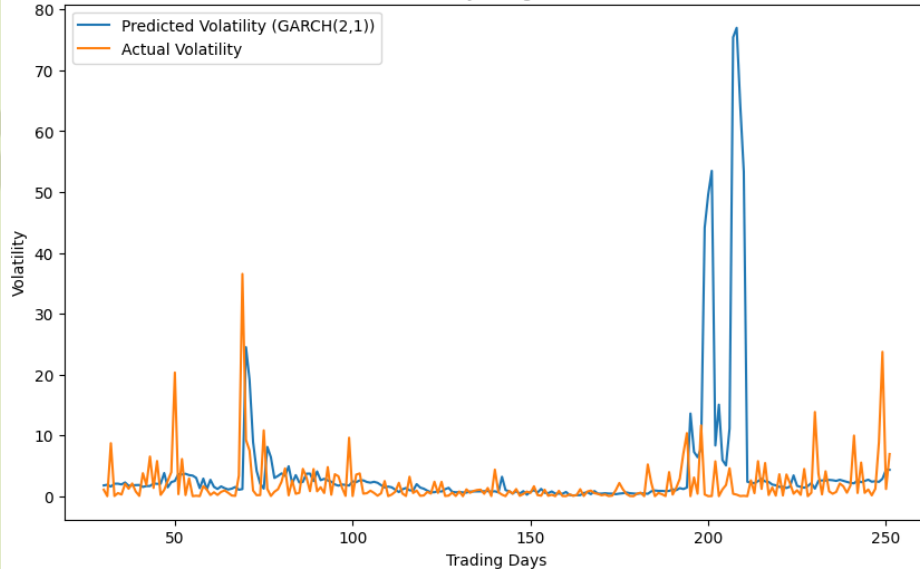




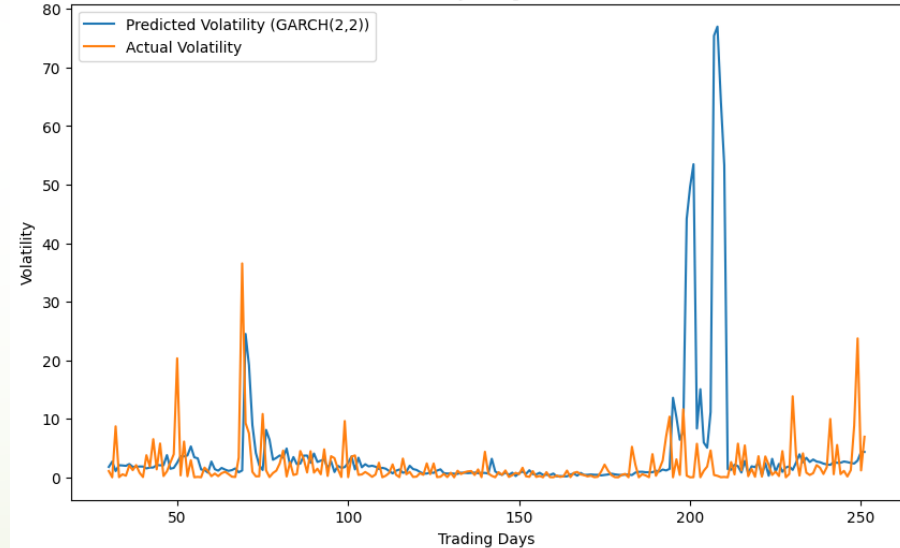
# Part I : Volatility estimation

**Fitted Garch Models :** The two best models regarding AIC and BIC

Predicted vs Actual Volatility using GARCH(2,1) for Year 2000



Predicted vs Actual Volatility using GARCH(2,2) for Year 2000



# Part I : Volatility estimation

**Fitted Garch Models** : The two best models regarding AIC and BIC

Model Comparison: MSE and Bias

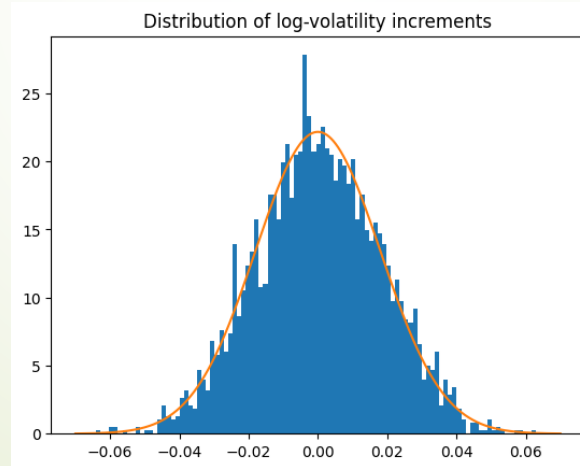
Model	MSE	Bias
GARCH(2,1)	134.90926498396993	2.0450884007989525
GARCH(2,2)	135.16597148422528	2.0277775158458846
GARCH(1,1)	135.47752829443598	1.9965653527420124
GARCH(1,2)	136.0164371999599	2.0271544478604118

# Part II : Rough volatility models

Fractional Ornstein-Uhlenbeck model for the log-volatility  $X_t$

$$dX_t = \nu dW_t^H + \alpha(m - X_t)dt$$

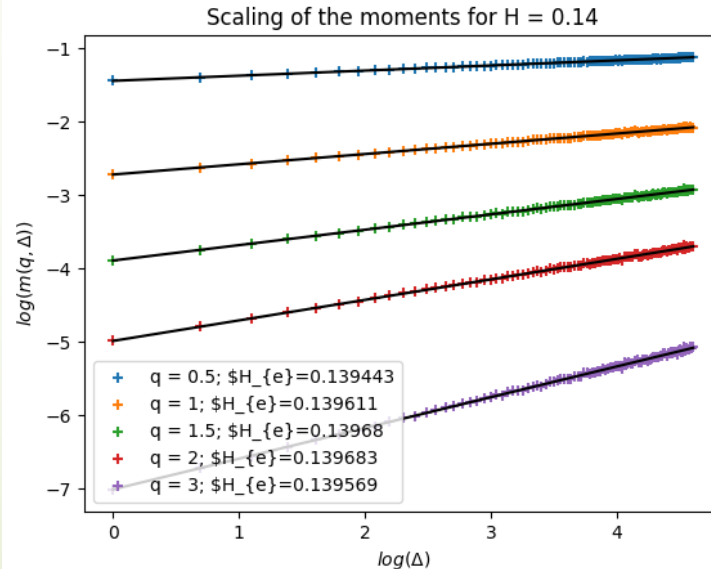
Where  $W_t^H$  follows a fractional Brownian motion



# Part II : Rough volatility models

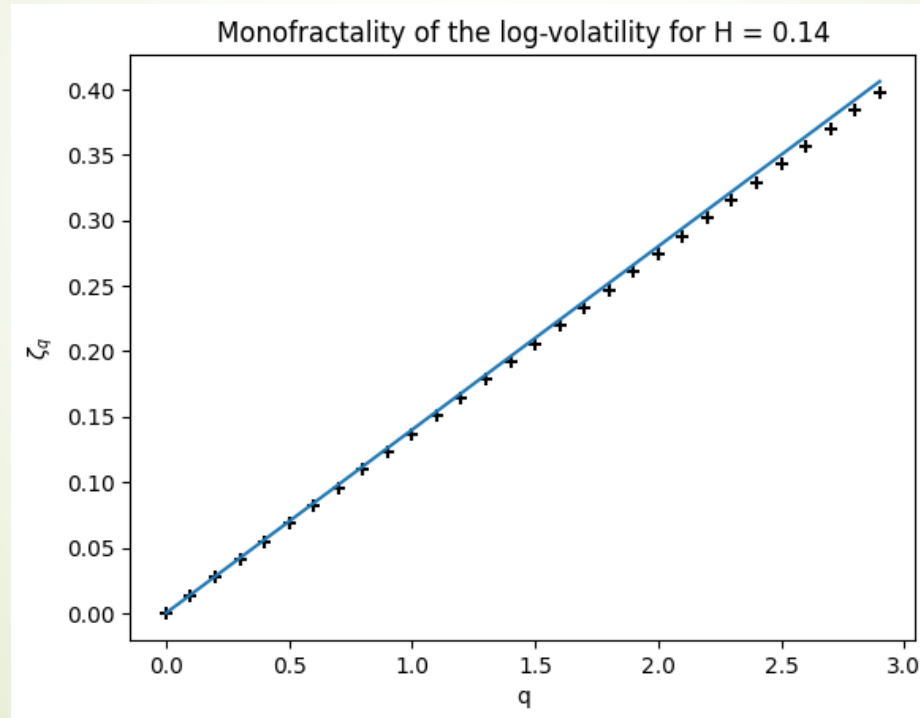
Measure of the regularity of the log-volatility

$$m(\Delta, q) = \mathbb{E}(|\log(\sigma t + \Delta) - \log(\sigma t)|^q)$$



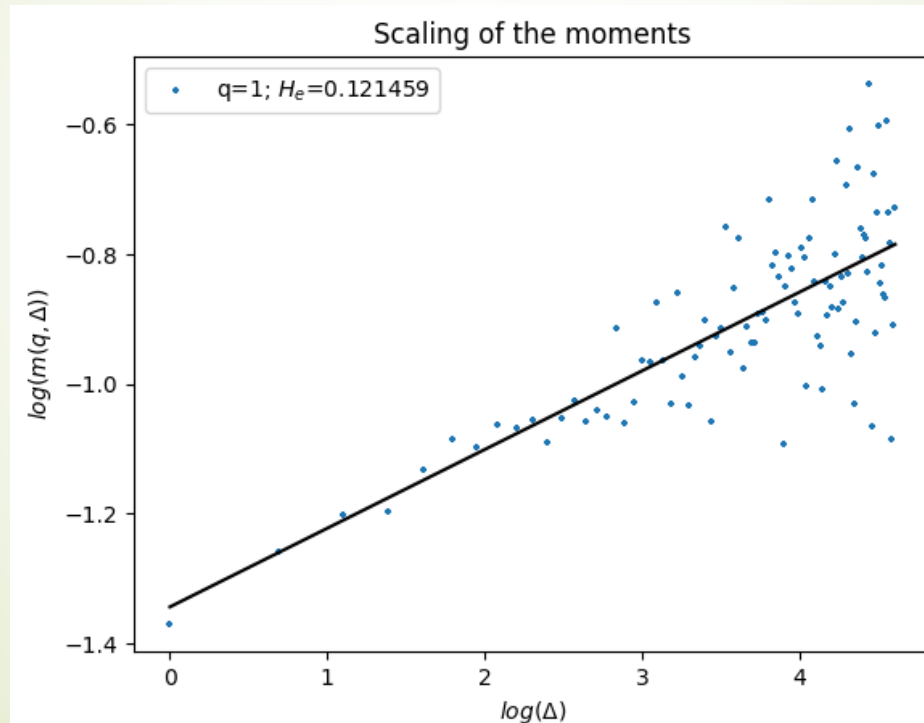
# Part II : Rough volatility models

## Monofractality of the log-volatility



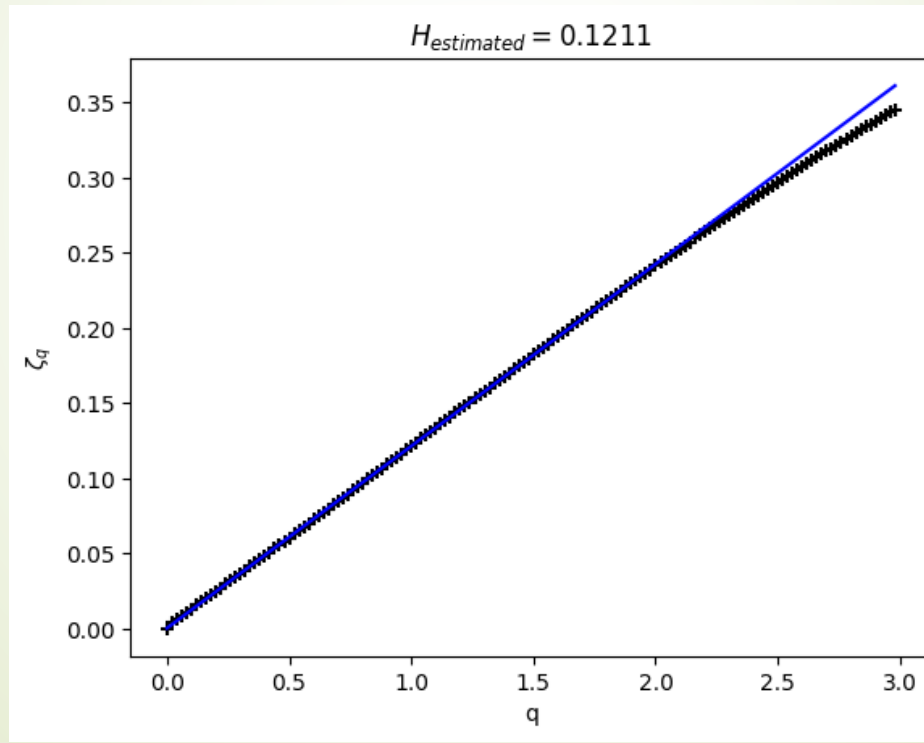
# Part II : Rough volatility models

## Tests with real market data



# Part II : Rough volatility models

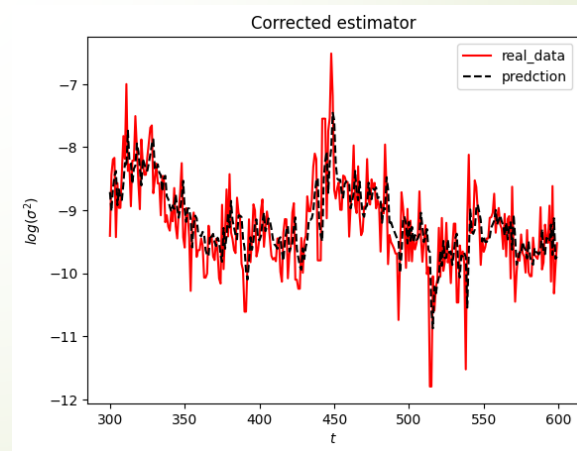
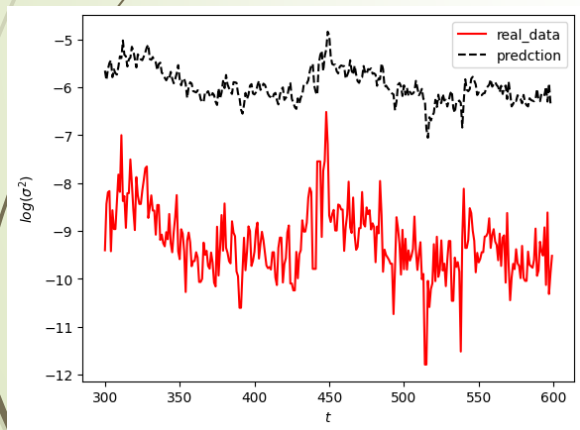
Tests with real market data



# Part II : Rough volatility models

## RFSV prediction

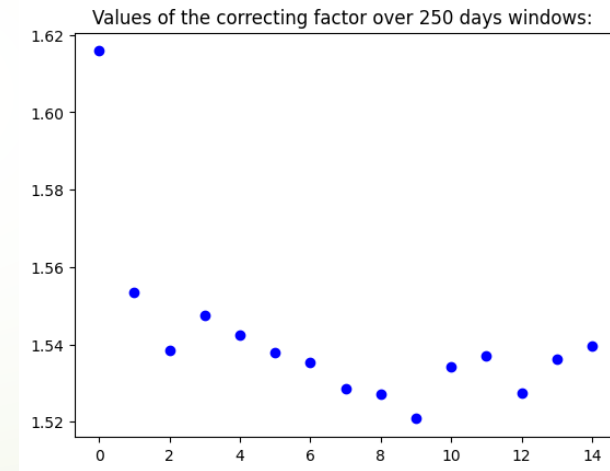
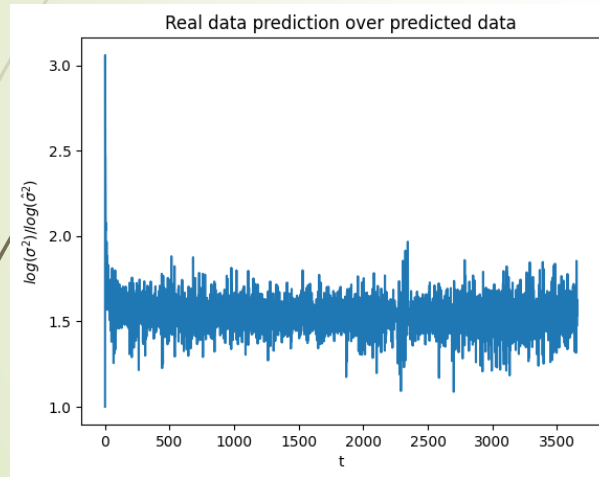
$$\mathbb{E} [\log \sigma_{t+\Delta}^2 \mid \mathcal{F}_t] = \frac{\cos(H\pi)}{\pi} \Delta^{H+1/2} \sum_{k=0}^N \frac{\log \sigma_{t-k}^2}{(k + \Delta + 1/2)(k + 1/2)^{H+1/2}}$$





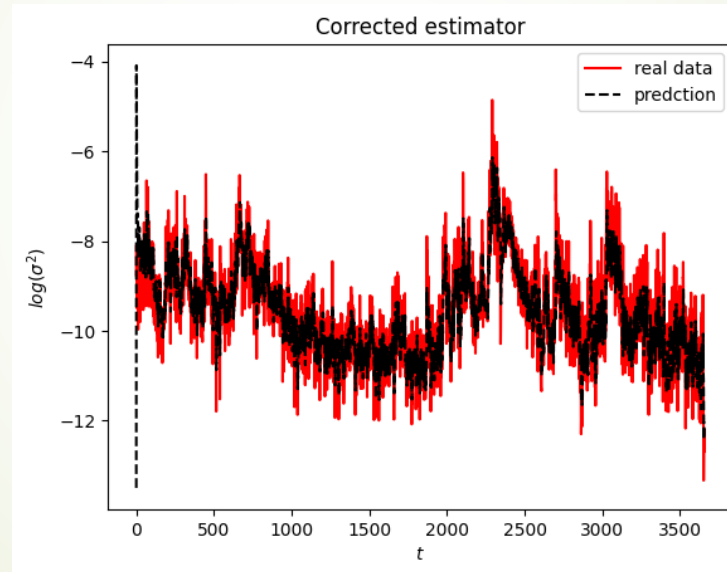
# Part II : Rough volatility models

RFSV prediction : determination of the correction factor



# Part II : Rough volatility models

RFSV prediction : Mean Square Error

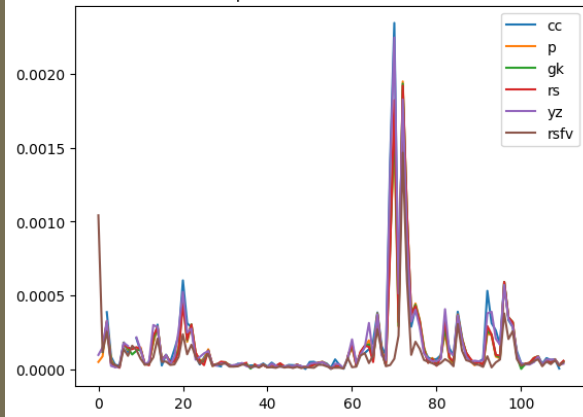


$$\text{MSE} = 1.35 \times 10^{-7}$$

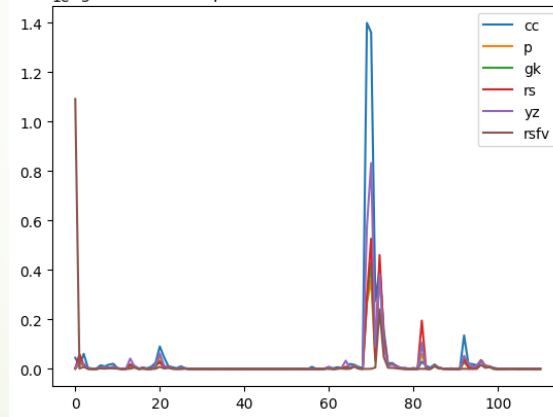
# Part II : Rough volatility models

## RFSV prediction : Comparison with other predictors

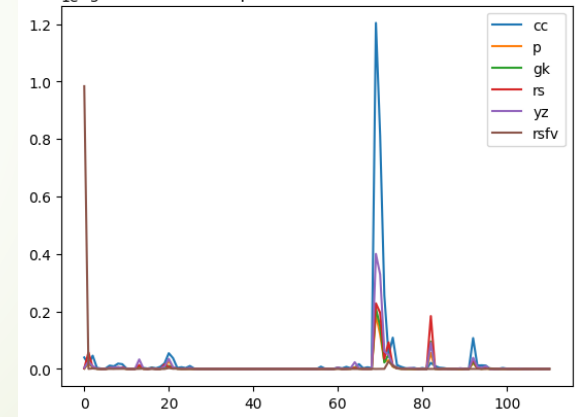
Bias computed over a 30 values window



MSE computed over a 30 values window



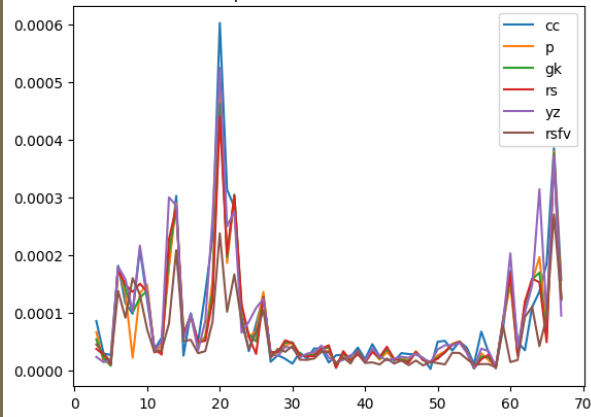
Variance computed over a 30 values window



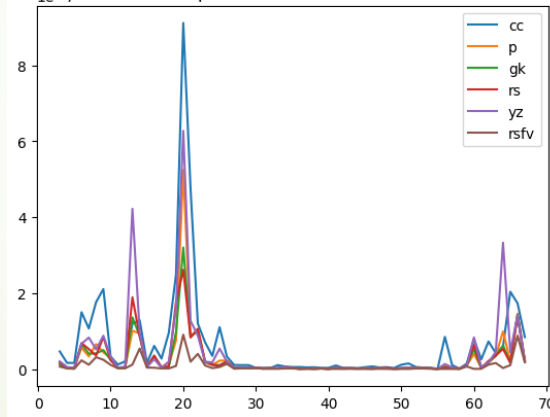
# Part II : Rough volatility models

## RFSV prediction : Comparison with other predictors

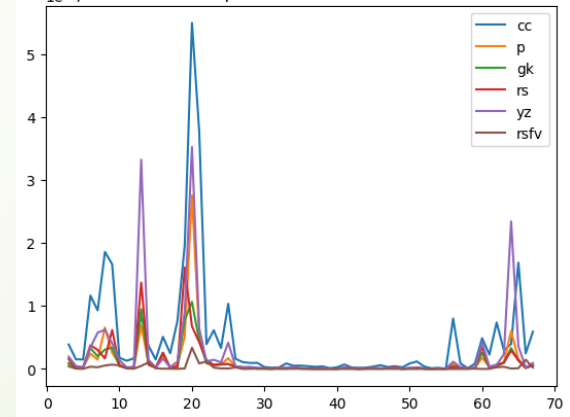
Bias computed over a 30 values window



MSE computed over a 30 values window

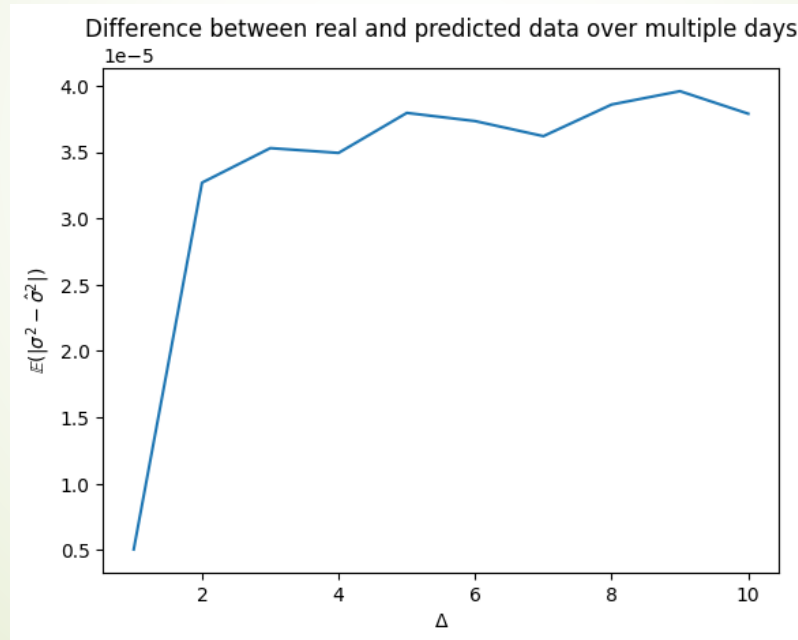


Variance computed over a 30 values window



# Part II : Rough volatility models

RFSV prediction : Prediction over multiple days

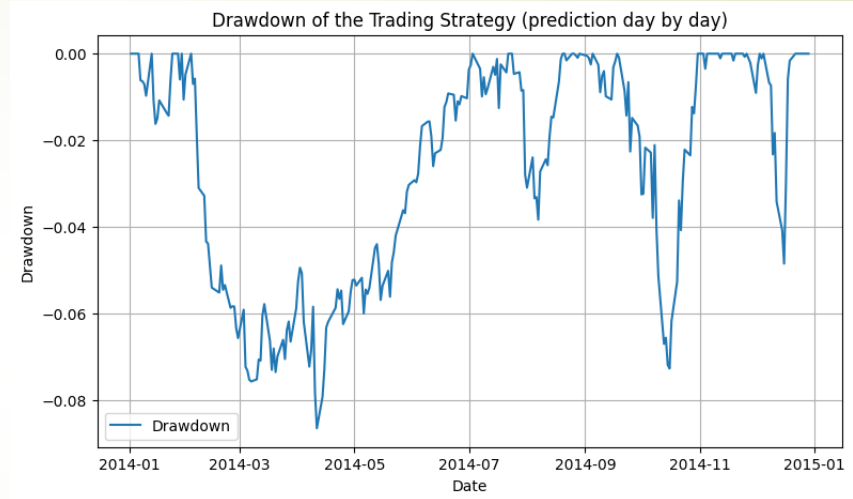
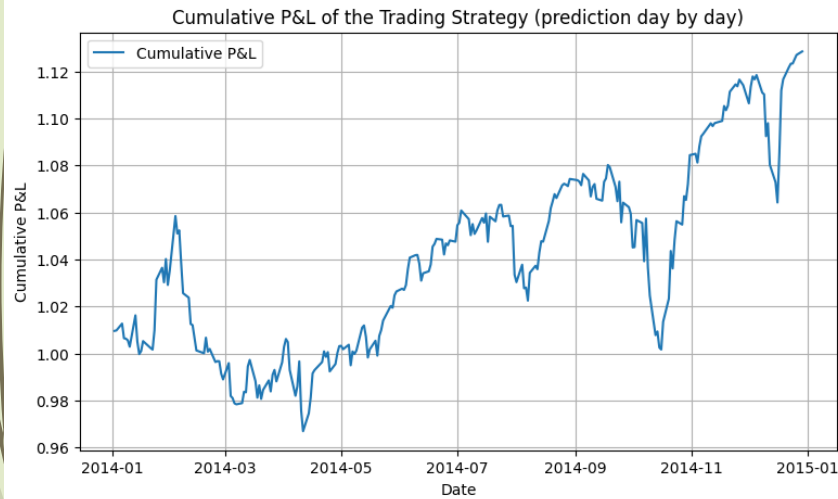


## Part III : Trading Strategy (risk management)

The idea is to be able to predict the intraday volatility for the next year and based on that, trade the SPY only during low volatility periods

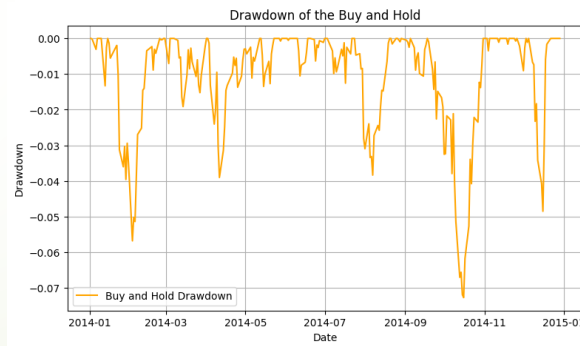
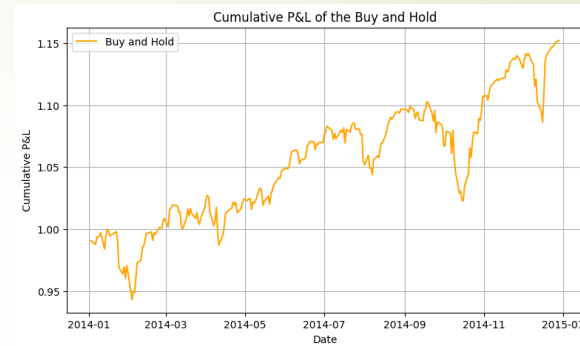
1. Estimate next day the volatility with “Rough Volatility” predictor with a sliding window of 3 years
2. Based on the predicted volatility we give the trading signal
  - 1: Buy if the volatility of the next day is predicted to be lower than the the mean of the last year
  - 1: Sell if the volatility of the next day is predicted to be higher than the the mean of the last year

# Part III : Trading Strategy (results)



Sharpe Ratio	Max Drawdown	Standard Deviation of Returns	Value-at-Risk (VaR) at 95.0% confidence level	Conditional Value-at-Risk (CVaR)
1.14	-0.086	0.007	-0.011	-0.0158

# Part III : Trading Strategy (results comparison)



Sharpe Ratio	Max Drawdown	Standard Deviation of Returns	Value-at-Risk (VaR) at 95.0% confidence level	Conditional Value-at-Risk (CVaR)
1.14	-0.086	0.007	-0.011	-0.0158

Sharpe Ratio	Max Drawdown	Standard Deviation of Returns	Value-at-Risk (VaR) at 95.0% confidence level	Conditional Value-at-Risk (CVaR)
1.328	-0.072	0.007	-0.011	-0.0171



# Conclusion

- ✗ Comparing the volatility estimators
- ✗ GARCH(2,1) or (2,2) results in a big peak of volatility compared to the actual values (not efficient)
- ✗ Rough volatility approach outperform the other estimators, especially when it comes to modelize peaks

## Possible improvements

- 1) Improve by estimating next day volatility taking into account the last trade-day and last 3 years and give the trading signal for the next day.
- 2) Compare the same strategy with the buy and hold on different periods.

**Thank you for your attention!!**